(i) 
$$\sqrt{x} = \frac{3+x}{\sqrt{12}}$$

 $3^{x^2} = 27^{x+1}$  correct to **two** decimal places.

(7 marks)

- (b) Convert:
  - 3.21∠5.37 radians to cartesian form; (i)
  - $x^2 y^2 = 16$  to polar form. 7. Na3)3/492. (6 marks)

140 - 360

- The cost of 5 resistors, 4 capacitors and 1 diode is Ksh 340; the cost of 10 resistors, 9 (c) capacitors and 4 diodes is Ksh 880; while the cost of 10 resistors, 13 capacitors and 15 diodes is Ksh 1920. Use elimination method to determine the cost of each component. (7 marks)
- 2. The word 'OPTICAL' is to be arranged so that the vowels always appear together. (a) Determine the number of possible ways in which this can be done. (4 marks)
  - Use the binomial theorem to expand  $(\frac{1-2x}{1+3x})^{\frac{1}{3}}$  upto the term in  $x^2$ . Hence, evaluate  $(\frac{0.98}{1.03})^{\frac{1}{3}}$  correct to **four** decimal places. (b) (i)

(10 marks)

- The second moment of area of a rectangle through its centroid is given by  $I_0 = \frac{bl^3}{12}$ , (c) where b is the width and l is the length. Use the binomial theorem to determine the approximate change in second moment of area if b increases by 2.5% and l decreases by 1.5%. (6 marks)
- Given the complex numbers  $Z_1 = 6j$  and  $Z_2 = 3 + j$ , determine  $\frac{Z_1}{Z_2}$ , expressing the (a) answer in exponential form. (5 marks)
  - Solve the equation  $Z^3 2 + j = 0$ , giving the answer in the form a + jb. (b)

(9 marks) 2=[2-5(3)

(c) ( Use Demoivre's theorem to show that:

$$\tan 3\theta = \frac{3\tan\theta - \tan^3\theta}{1 - 3\tan^2\theta} \qquad Z = \left(Y \left[1 - \cos\theta\right]\right)^{\alpha} \qquad (6 \text{ marks})$$

- 4.
- Solve the equation  $\log(x^2 + 6) \log x = \log 5$ . (a)

- (3 marks)
- Find the value of  $\tan \theta$ , given that  $\sin(\theta + 45^{\circ}) = 3\cos(\theta + 45^{\circ})$ . (b)
- (4 marks)
- Solve the equation  $4\cos 2\theta 2\sin \theta + 2 = 0$  for  $0^{\circ} \le \theta \le 360^{\circ}$ . (c)
- (6 marks)
- The longest side of a right angled triangle is (x + 9) cm. If the lengths of the other (d) remaining sides are (x + 5) cm and (2x + 6) cm, determine the:
  - dimensions of the triangle; (i)
  - (ii) area of the triangle.

(7 marks)

- Find the inverse of the function  $f(x) = \frac{3x+2}{x-2}$ . 5. (a)
- (3 marks)
- Given that  $Ae^x Be^{-x} = 8 \cosh x 2 \sinh x$ , find the values of A and B. (b)
- (3 marks)

- (c) Prove the hyperbolic identities:
  - $\tanh(\theta \phi) = \frac{\tanh \theta \tanh \phi}{1 \tanh \theta \tanh \phi}$
  - $\frac{\sinh^2\theta + \cosh^2\theta 1}{4\cosh^2\theta \coth^2\theta} = \frac{1}{2}\tanh^4\theta$

(7 marks)

- Solve the equation  $4\cosh 2x = 4 + 2\sinh 2x$  giving the answer correct to three decimal (d) places. (7 marks)
- Given  $y = \sin(2x+3)$ , find  $\frac{dy}{dx}$  from first principles. 6. (a)

(5 marks)

Given that  $y = ln\left(\frac{1-x^2}{1+x^2}\right)$ , show that  $\frac{dy}{dx} = \frac{-4x}{1-x^4}$ . (6)

(6 marks)

- The power developed in a resistor R by a battery of emf E and internal resistance r is (c) given by  $P = \frac{E^2R}{(R+r)^2}$ . SRP+Y
  - (i) find  $\frac{dp}{dR}$ ;
  - (ii) show that the power is maximum when R = r.

(9 marks)

7. (a) If  $Z = \frac{x}{y} \ln y$ , show that  $\left(\frac{1}{y \ln y} - \frac{1}{y}\right) \frac{\partial z}{\partial x} = \frac{\partial^2 z}{\partial x \partial y}$ .



- (b) Given that the volume of a cone is  $V = \frac{1}{3}\pi r^2 h$ , use partial differentiation to determine the approximate change in volume if the radius increases from 5 cm to 6 cm, and the height decreases from 4 cm to 3.5 cm. (6 marks)
- (c) Locate the stationary points of the function  $Z = 2x^2 3y^2 + 8xy 4x + 6y + 6$  and determine their nature. (9 marks)
- 8.
- (a) Evaluate the integrals:
  - (i)  $\int (3x-5)^4 dx$
  - (ii)  $\int \sin^2 3x \, dx$
  - (iii)  $\int_{6}^{7} \frac{18 + 21x x^{2}}{(x 5)(x + 2)^{2}} dx$

(12 marks)

(b) Figure 1 shows a sketch of the graph of the function  $y = e^x$ .

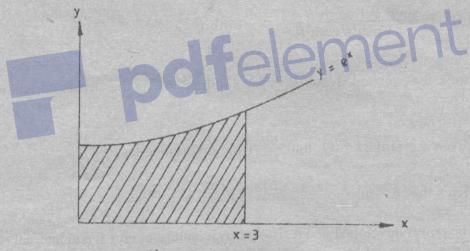


Fig. 1

Determine the:

- (i) area enclosed by the curve, the x-axis, the y-axis and the ordinates x = 3.
- (ii) centroid of the area in (i) above.

(8 marks)

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