1521/203 1601/203 1522/203 1602/203 MATHEMATICS II Oct/ Nov. 2016 Time: 3 Hours



## THE KENYA NATIONAL EXAMINATIONS COUNCIL

## CRAFT CERTIFICATE IN ELECTRICAL AND ELECTRONIC TECHNOLOGY (POWER OPTION) (TELECOMMUNICATION OPTION) MODULE II

MATHEMATICS II

3 hours

## INSTRUCTIONS TO CANDIDATES

You should have mathematical tables/ non-programmable scientific calculator for this examination: Answer FIVE of the following EIGHT questions in the answer booklet provided. All questions carry equal marks.

Maximum marks for each part of a question are as shown. Candidates should answer the questions in English.

This paper consists of 4 printed pages.

Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no question is missing.

- 1. (a) Write down the middle term in the binomial expansion of  $(4x + 3y)^8$ , and determine its value when  $x = \frac{1}{3}$  and  $y = \frac{1}{4}$ . (7 marks)
  - (b) Find the first four terms in the binomial expansion of  $\left(1 + \frac{1}{2}x\right)^{1/2}$ , and state the values of x for which the expansion is valid. (5 marks)
  - (c) (i) Expand  $(1+x)^{1/2}$  as far as the term in  $x^3$ .
    - (ii) By setting  $x = \frac{1}{8}$  in the result in (i), determine the value of  $\frac{1}{2\sqrt{2}}$ , correct to four decimal places.

112", 112", 313, 112" 33", 112" 313, 112" 313

(8 marks)

- 2. (a) Given  $\sin A = \frac{4}{5}$  and  $\cos B = \frac{12}{13}$ , where A and B are acute, determine the values of:
  - (i) sin (A B);
  - (ii) tan (A + B).

(7 marks)  $1 \pm 31 = 1, 6, 6, 6, 1$  $1 \pm 6 \pm 1 = (0.4) \times 44 (4 \times 78)^{1/4} + 6$ 

(b) Prove the identities:

- (i)  $\frac{1+\sin\theta}{\cos\theta} + \frac{\cos\theta}{1+\sin\theta} = 2\sec\theta$
- (ii)  $\sin 3\theta = 3\sin \theta 4\sin^3 \theta$ .

(6 marks)

- (c) Given that  $t = \tan 22 \frac{1}{2}^{\circ}$ , use the formula for  $\tan 2\theta$  to show that  $t^2 + 2t 1 = 0$ .
  - (ii) Hence, by solving the equation in (i), determine the value of  $\tan 22\frac{1}{2}$ , giving the answer in surd form.

(7 marks)

- 3. (a) By completing the square, determine the values of r, s and t such that  $3x^2 + 4x + 10 = r(x+s)^2 + t$ . (5 marks)
  - (b) Solve the equation:

 $3^{2r+1}-11(3^r)+6=0$ , correct to two significant figures.

(6 marks)

Currents I1, I, and I2 in an electric circuit satisfy the simultaneous equations:

$$I_1 - 2I_2 + 2I_3 = 3$$
  
 $2I_1 + 3I_2 - I_3 = 7$   
 $-3I_1 + 4I_2 + 5I_3 = 29$ .

Use elimination method to determine the values of the currents.

(9 marks)

- Given the vectors  $\mathbf{A} = 3i 2j + k$ ,  $\mathbf{B} = -i + 3j + 4k$ , determine the:
  - (i) angle between A and B;
  - (ii) area of the parallelogram spanned by the vectors A and B.

(10 marks)

- The electric field  $E = x^{i}i + z^{i}j + y^{i}k$  exists in a region of space. Determine, at the 1×14-3×-1+1×1 0x-11-3x1101 point (-1, 2, 1):
  - VXE:
  - (ii) V.E.

(10 marks)

- Given the matrices  $A = \begin{bmatrix} 1 & -3 & 1 \\ -1 & 1 & 3 \\ 1 & 2 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 & -1 & 1 \\ -1 & 2 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ , determine  $(AB)^{-1}$ . (9 marks)
  - Three forces F1, F2 and F3 in a mechanical system satisfy the simultaneous equations (b)

$$2F_1 - F_2 + 3F_3 = 7$$
  
 $F_1 + F_2 - F_3 = 0$   
 $-F_1 + F_2 + 2F_3 = 4$   
 $3 \cos x - 2 \sin x + 1) dx$   
amer's rule to solve the equations (11 mg)

Use Cramer's rule to solve the equations.

- 6. (a) Prove the identities:
  - $\frac{\sin B \sin C}{\sin B + \sin C} = \cot \left(\frac{B + C}{2}\right) \tan \left(\frac{B C}{2}\right);$ (i)
  - $\cosh^3 x \sinh^3 x = 1$ . (ii)

(4 marks)

- (b) Solve the equations:
  - (i)  $3\cot 2x + \cot x = 1$ , for  $0^{\circ} \le x \le 360^{\circ}$ ;
  - $5\cosh\theta + \sinh\theta = 5$ . (ii)

(16 marks)

1521/203 1601/203 1522/203 1602/203 7. \* (a) Given  $y = \frac{1}{x+3}$ , find  $\frac{dy}{dx}$  from first principles.

(5 marks)

- (b) Use implicit differentiation to determine the equation of the tangent to the curve  $x^{2}-3y^{2}+4xy=6$  at the point  $\left(\frac{1}{2},\frac{1}{2}\right)$ . (7 marks)
- (c) Determine the stationary points on the curve y = x³ + 3x³ 72x + 6, and state their nature.
  (8 marks)
- 8. (a) Given  $z = \frac{x+y}{x-y}$ , show that  $x \frac{\partial^2 z}{\partial x^2} y \frac{\partial^2 z}{\partial y^2} = 0$ . (8 marks)

  - (c) Evaluate the integrals:
    - (i)  $\int_0^1 \frac{x^{-3} + 2x^{-2} + x^{-1}}{x^{-1}} dx; = \frac{x^{-2}}{x^{-1}} + 2x^{-1} + x$
    - (ii)  $\int_0^{\pi/2} (3\cos x 2\sin x + 1) dx$ .

(5 marks)

## THIS IS THE LAST PRINTED PAGE.

2 2 -1

1521/203 1601/203 1522/203 1602/203 Oct / Nov. 2016 4 1000